

4c) Find the total number of calories burned over $[6, 18]$

Total calories = initial calories + total change

$$= 0 + \int_6^{18} f(t) dt$$

(derivative or instantaneous r.v.c.)

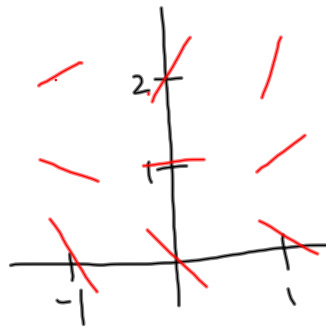
$$= \text{Area from } 6 \rightarrow 18 = 6 \cdot 9 + \frac{1}{2}(9+15)(4) + 2(15)$$

base height $h_1 + h_2$ 6 base height

$$= 54 + 48 + 30 = 132$$

2007/5

$$\frac{dy}{dx} = \frac{1}{2}x + y - 1$$



$$\text{at } (-1, 2) \quad \frac{dy}{dx} = -\frac{1}{2} + 2 - 1 = \frac{1}{2}$$

$$(-1, 1) \quad \frac{dy}{dx} = -\frac{1}{2} + 1 - 1 = -\frac{1}{2}$$

$$(-1, 0) \Rightarrow -\frac{1}{2} + 0 - 1 = -\frac{3}{2}$$

$$(0, 2) \Rightarrow 1$$

$$(0, 1) \Rightarrow 0$$

$$(0, 0) \Rightarrow -1$$

$$(1, 2) \Rightarrow \frac{3}{2}$$

$$(1, 1) \Rightarrow \frac{1}{2}$$

$$(1, 0) \Rightarrow -\frac{1}{2}$$

$$\begin{aligned} b) \quad \frac{d^2y}{dx^2} &= \frac{d}{dx} \left(\frac{1}{2}x + y - 1 \right) \\ &= \frac{1}{2} + \frac{dy}{dx} = \frac{1}{2} + \left(\frac{1}{2}x + y - 1 \right) \\ \frac{d^2y}{dx^2} &= \frac{1}{2}x + y - \frac{1}{2} \end{aligned}$$

c) at (0, 1)

$\frac{dy}{dx} = 0$. so it is a critical point.

as "x" moves, from 0, to the right

$\frac{dy}{dx} = \frac{1}{2}x + y - 1$ becomes positive
so function is increasing

as "x" moves left from 0,

$\frac{dy}{dx}$ becomes negative,
so function, to the immediate
left of $x=0$, is decreasing

Since $f(x)$ changes from decreasing to
increasing, $f(x)$ has a rel. min
at (0, 1)

Alternatively

$$\frac{d^2y}{dx^2} = \frac{1}{2}x + y - \frac{1}{2} \text{ at } (0, 1) \text{ is } \frac{1}{2}, \text{ so } f(x)$$

is concave up.

and therefore, $f(x)$ has a rel. min
at (0, 1)

2007 b continued

$$\frac{d^2y}{dx^2} = \frac{1}{2}x + y - \frac{1}{2}$$

The solution curves are concave up
when $\frac{d^2y}{dx^2}$ is positive.

i.e. $\frac{1}{2}x + y - \frac{1}{2} > 0$

$$\frac{1}{2}x + y > \frac{1}{2}$$

$$y > \frac{1}{2}(1-x)$$



d) $y = mx + b$

$$\frac{dy}{dx} = m$$

this is a solution to our diff. eq.

when $\frac{dy}{dx} = \frac{1}{2}x + y - \frac{1}{2} = m$

i.e. $y = \left(-\frac{1}{2}x + \frac{m+1}{2}\right) = mx + b$

$$m = -\frac{1}{2}; b = \frac{m+1}{2} = \frac{-\frac{1}{2}+1}{2} = \frac{1}{4}$$

2009B
1C

$$\int_0^3 A'(t) dt = A(3) - A(0) \text{ by FTC}$$

$A(t)$ is an antiderivative of $A'(t)$.

Accumulation idea $\int_0^3 A'(t) dt$ is

the \int total change in area between $\begin{bmatrix} 0 \\ 3 \end{bmatrix}$
 $t=0$ years and $t=3$ years

total area = starting 36π area
 + total change in area

radius at $t =$ radius at 0 $\rightarrow 6$
 + total change in radius from 0 $\rightarrow t$ $\int_0^3 \frac{1}{6}(3+5t) dt$

